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# **A thermodynamic analysis of the first solvation shells of alkali and halide ions in liquid water and in the gas phase**

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Let *n* denote the number of water molecules in the nearest-neighbour shell (NS) of an ion  $J^{\pm}$  in liquid water, and denote  $J^{\pm} \cdot nH$ , O in the gas phase by  $J^{\pm} \cdot NSG$  (g). The standard free energy of hydration  $\Delta G_{\text{hyd}}^0$  ( $J^{\pm}$  -NSG) can then be deduced by a thermodynamic cycle involving  $\Delta G_n^0$  for the formation of  $J^{\pm}$  **NSG** (g) and  $\Delta G_{\text{hvd}}^0$ for the transfer of  $J^{\pm}$  (g) to water. Values of  $\Delta G_{\text{hvd}}^0$  ( $J^{\pm}$  -NSG) for alkali and halide ions are substantial, ranging from 48% to 86% of  $\Delta G_{\text{bwd}}^0$ . The values of  $\Delta G_{\text{bwd}}^0$  $(J^{\pm} \cdot \text{NSG})$  can be accounted for largely by the calculated work-electrostatic  $(\Delta W_{elec})$  and surface  $(\Delta W_{surf})$ —in the process  $J^{\pm} \cdot \text{NSG (g)} \rightarrow J^{\pm}$  (aq).  $\Delta W_{elec}$  is the major contributor.  $\Delta W_{\text{surf}}$  depends on whether (i)  $J^{\pm}$  **NSG** (g) can be represented by a cluster consisting of the ion and *n* separate water molecules, or (ii) there is some molecular complex formation within that cluster. In fact,  $\Delta W_{\text{surf}} < 20 \text{ kJ}$ mol<sup>-1</sup> for the alkali ions and of the order of 100 kJ mol<sup>-1</sup> for the halide ions. A reasonable case can be built that the alkali ions and some of the *n* water molecules form molecular complexes while the anions are better represented by case (i).

#### **1. Introduction**

One approach to ionic hydration is to study the stepwise association of the ion with water molecules in the gas phase—for instance in the case of alkali ions  $(M^{\dagger})$ ,

$$
M^{+}(g) + w H_{2}O(l) \to M^{+} \cdot (H_{2}O)_{w}(g); \quad \Delta G_{w}^{0}(M^{+})
$$
 (1)

and allow *w* to grow large enough to represent a macroscopic liquid cluster. This approach is exemplified by the elegant work of Kebarle and co-workers (Dzidic and Kebarle 1970, Arshadi *et al.* 1970). Another approach is to measure  $\Delta G_{\text{hyd}}^0$  for the transfer of an electrically neutral combination—for instance,  $M^+ + X^-$ , from the gas phase to liquid water, and use the Born equation, or some modification of it (for references see table **3),** to dissect the measurement into additive terms for the separate ionic species,  $\Delta G_{\text{hyd}}^0 (M^+ + X^-) = \Delta G_{\text{hyd}}^0 (M^+) + \Delta G_{\text{hyd}}^0 (X^-)$ , where

$$
M^{+}(g) + aq \rightarrow M^{+}(aq); \quad \Delta G^{0}_{\text{hyd}}(M^{+})
$$
 (2)

In equation (2) and the following, 'aq' denotes an unspecified amount of liquid water, and  $M<sup>+</sup>$  (aq) denotes the solvated alkali ion at equilibrium in liquid water. More generally in what follows we shall represent the alkali or halide ions by a common symbol  $J^{\pm}$ .

Both approaches can focus on the nearest-neighbour shell **(NS)** to the ion. Stepwise association in the gas phase can allow *w* to increase **up** to the number, *n,* of water molecules in the NS of  $J^{\pm}$  *in liquid water*. The result,  $J^{\pm}$  (H<sub>2</sub>O)<sub>n</sub>, will be denoted by **J' \*NSG;** it represents a hydrated ion in the gas phase with an equilibrium water shell which is isomeric, but perhaps not identical, with that of the nearest-neighbour shell of the ion in liquid water. The latter we shall designate **NSL.** Since the water **structure** in the **NS** should be mainly controlled **by** the central ion, we shall at present assume that **NSG** = **NSL**. In figure 1 we denote  $\Delta G^0$  for the formation of  $J^{\pm} \cdot \text{NSG}$  (g) from  $J^{\pm}$  (g) and  $nH_2O$  (l) by  $\Delta G_n^0$  ( $J^{\pm}$ ).



Figure 1. Relationship between the free energy of hydration of the 'bare' ion,  $J^{\pm}$  (g), and the ion with water filling its nearest-neighbour shell,  $J^{\pm}$  · NSG (g).

Kebarle and co-workers plotted cation-cation differences and anion-anion differences  $\delta \Delta G_w^0$  versus *w*. As *w* becomes large, such plots approach the corresponding values of  $\delta \Delta G_{\text{hvd}}^0$ , thus satisfying a condition for thermodynamic consistency between gas-phase and liquid-phase hydration. In this paper, on the other hand, we intercompare cations with anions and examine the absolute hydration free energies of the gaseous ion hydrates,  $\Delta G_{\text{hyd}}^0$  (J<sup> $\pm$ </sup> · NSG). We find that the latter are very substantial, varying from 48 % to 86 % of  $\Delta G_{\text{hvd}}^0$  (J<sup>+</sup>), the hydration free energy of the 'bare' ion.

In the following we shall use the symbol **W** for *calculated* work (electrostatic or surface) done on the system. Thus, for example, if W<sub>elee</sub> (g) is the work done in creating the electrical field associated with  $J^{\pm}$  **NSG** (g) and  $W_{elec}$  (aq) is the work done in the electrical field associated with  $J^{\pm} \cdot \text{NSG}$  (g) and  $W_{\text{elec}}$  (aq) is the work done in creating the field associated with  $J^{\pm}$  (aq), then  $\Delta W_{\text{elec}} = W_{\text{elec}}$  (aq) $-W_{\text{elec}}$  (g), with a  $\sin^2\theta = \Delta W_{\text{surf}}$ . This means that  $\Delta G_{\text{hyd}}^0(\vec{J}^{\pm} \cdot \text{NSG}) = \Delta W_{\text{elec}} + \Delta W_{\text{surf}}$ . We shall show that for  $J^{\pm}$  **NSG** (g), the electrostatic part of the hydration free energy,  $\Delta W_{\text{elec}}$ , is within the scope of the Born equation (1920). Surface work must also be considered because the species  $J^{\pm}$  **·NSG** (g) may be considered as a water 'droplet' with a high surface/volume ratio. The ability to use classical equations for the surface free energy of a droplet of the dimensions of  $J^{\pm}$  **NSG** (g) is open to question and we shall say more about this later in the paper.

Let us assume that the number *n* of water molecules in the **NS** can be predicted. Then  $\Delta G_n^0$  (J<sup> $\pm$ </sup>) can be obtained from the papers of Kebarle *et al.* after converting the starting state from H<sub>2</sub>O (g) to H<sub>2</sub>O (l).  $\Delta G_{\text{hyd}}^0$  (M<sup>+</sup>) and  $\Delta G_{\text{hyd}}^0$  (X<sup>-</sup>) are known from the dissection of experimental values of  $\Delta G_{\text{hyd}}^0$  for the neutral combinations of ions. Figure 1 then shows how this information can be used to determine  $\Delta G_{\text{hvd}}^0$  (J<sup> $\pm$ </sup> · NSG). Figure **2,** which will be discussed in greater detail later, displays the species shown in figure 1 more pictorially.



Figure 2. Schematic of *(a)* a 'bare' ion,  $J^{\pm}$  (g), *(b)* an ion with its nearest-neighbour shell (NS) filled with water,  $J^{\pm}$  ·NSG (g), and *(c)* an ion dissolved in water,  $J^{\pm}$  (aq). In *(c)*  $D_M(r)$  is the dielectric constant of the surrounding medium at distance *r* from the centre of the ion. Beyond NS,  $D_M(r)$  is close to its low-field value of 78.3 (water). In *(b)*, beyond NS,  $D_g(r)$ is close to 1, but this is not so inside NS. Inside the NS of  $(b)$  and  $(c)$  we may expect  $D_{\rm M}(r) \sim D_{\rm g}(r)$ .

#### **2. Comparison with stepwise hydration in the gas phase**

Experimental results for  $\Delta G_w^0$  (J<sup>+</sup>) (equation (1)) for alkali and halide ions are listed on the left side of table 1. The values are those reported by Dzidic and Kebarle (1970) and by Arshadi, Yamdagni and Kebarle (1970) but have been corrected by us for the standard free energy of condensation of water, since figure 1 requires  $H_2O$  (1) rather than H<sub>2</sub>O (g) as reactant. The stepwise hydration numbers  $w$  go up to 4, 5, or 6. Measurement beyond the highest reported w was impractical.

For comparison with the nearest-neighbour shell **(NS)** of the ion in liquid water, we need  $\Delta G_n^0$  (J<sup> $\pm$ </sup>), where *n* is the number of water molecules in the NS in liquid water. The thickness of the nearest-neighbour shell (NS) is close to 2.4 **A,** obtained by adding the radius of the water molecule,  $1.4 \text{ Å}$ , to half the distance between the first and second peak in the radial distribution function of liquid water (Narten and Levy 1969). Thus  $r_2 = r_1 + 2.4$  Å, where  $r_1$  is the hard-sphere radius of the ion. Values of  $r_1$  and  $r_2$  for alkali and halide ions are listed in table 2. Given these values, letting  $V_{H_00} = 18 \text{ mL}$  $mol<sup>-1</sup>$ , and assuming that the electrostriction of the water around an ion is localized in the NS, we calculate *n* as the integer nearest to the value of  $f$  in equations (3).

$$
f = \left[4\pi N_A (r_2^3 - r_1^3)/3 + \Delta V_{\text{electrostric}}\right] / 18\tag{3a}
$$

$$
\Delta V_{\text{electrostric}} = (4/3)\pi N_A r_1^3 / 0.55 - V_{\text{ion}}.
$$
\n(3b)

In (36) the first term on the right estimates the ionic volume in the absence of electrostriction, using a filling factor of 0.55.  $V_{ion}$  is the ionic partial molar volume as given in the review by Marcus (1994). Values of 18frange from **80** to 220 mL mol-l; those of  $\Delta V_{\text{electrostrict}}$  range from 4 to 12 mL mol<sup>-1</sup>. The results for *n* are included in table 1.

For Li<sup>+</sup> and Na<sup>+</sup>, *n* is within the experimental range of Dzidic and Kebarle (1970), and  $\Delta G_n^0$  is an experimental number. For the other ions, extrapolation of the experimental  $\Delta G_w^0$  to  $w = n$  is required. Fortunately the extrapolation is small. To make the extrapolation as smooth as possible, we fitted the available  $\Delta G_w^0$  to the empirical equation,  $\Delta G_w^0 = a + bw + cw^{-1/5}$  (where *a, b, c* are parameters of fit), and extrapolated to  $w = n$ . The results are listed in table 1. For consistency, we fitted the data for  $Li^+$  and Na<sup>+</sup> similarly and interpolated at  $w = n$ . As can be seen from figure

Ion	$-\Delta G_1^0$	$-\Delta G_{2}^{0}$	$-\Delta G_{3}^{0}$	$-\Delta G_4^0$	$-\Delta G_{5}^{0}$	$-\Delta G_6^0$	n	$-\Delta G_n^0(\mathbf{J}^{\pm})$
$Li+$	98	169	216	238	249	250	5	249
$Na+$	65	112	142	160	168	171	6	173
$K^+$	39	68	86	95	100	101	8	105
$Rb^+$	32	52	65	72	75		8	84
$Cs+$	24	40	50	54	57		9	61
$F^-$	67	105	128	142	163			190
$Cl^-$	26	44	54	60			10	76
$Br^-$	21	35	44	47			11	57
$I^-$	14	23	27	(30.5)			12	39

**Table** 1. **Stepwise hydration of gaseous ions at** 298 K."

<sup>*a*</sup> All free energies in kJ mol<sup>-1</sup>.

Table 2. Ion parameters and ionic free energies of hydration at  $298 \text{ K}^d$ 

Ion	Radius of NS $(\AA)^b$		Inner $(r_1)^c$ outer $(r_2)$ $-\Delta G_{\text{hyd}}^0$ $({\rm J}^{\pm})^{a.c}$	$-\Delta G_{\rm hyd}^0 (J^{\pm} \cdot \rm NSG)$		
$Li^{+}$	0.69	3.09	475	226		
$Na+$	1.02	$3-42$	365	192		
$K^+$	1.38	3.78	295	190		
$Rb^{+}$	1.49	$3-89$	275	191		
$Cs^+$	$1-70$	4.10	250	189		
$F^-$	1.33	3.73	465	275		
$Cl^-$	1.81	4.21	340	264		
$Br^-$	1.96	4.36	315	258		
I-	2.20	4.60	275	236		

**<sup>a</sup>These values use the same concentration units in gas and liquid**  phase and are independent of concentration units.

*r*<sub>2</sub> =  $a + 2.4$  Å.

**Data tabulated by Marcus** (1994).

**All energies in kJ** mol-I.

1, these values together with the values of  $\Delta G_{\text{hyd}}^0$  **(J<sup>±</sup>)** from table 2 allow the determination of  $\Delta G_{\text{hyd}}^0$  (J<sup> $\pm$ </sup> · NSG), whose values are given in table 2. The first point to notice **is** that *these ions stillhave very substantial free energies of hydration, ranging from 48* % *to as much* **as** *86* % *oj the hydration free energy of the 'bare' ions.* **Also** for similar values of  $r_2$ , the magnitude of  $\Delta G_{\text{hyd}}^0$  (X<sup>-</sup>·NSG) exceeds that of  $\Delta G_{\text{hyd}}^0$  (M<sup>+</sup>·NSG) by about 100 **kJ** mol-'. We shall now see if we can account for these results.

## **3. Calculation of hydration free energies**

## 3.1. *Electrical work and the Born equation*

The dissection of measured standard free energies of hydration **for** neutral *pairs,*   $M^+ + X^-$ , into separate terms for  $M^+$  and  $X^-$  has been giving robust results (within 20 kJ mol<sup>-1</sup>) since feasibility was demonstrated in a classic paper by Latimer, Pitzer and Slansky **(1939).** Key methods and results are shown in table 3. All of the treatments are inspired by the Born equation, but they differ in approach and detail. The approaches include elements of electrostatics, electrochemistry, physical chemistry, and physical-organic chemistry.

Date	Source		$\Delta G^0$ (kJ mol <sup>-1</sup> ) $\Delta H^0$ (kJ mol <sup>-1</sup> )	
1920 1939	Born, citing Fajans Latimer et al., Born equation with adjusted	$-1050+10$	$\Delta U - 1100$ $-1100 + 101.5$	
	radii			
1962	Noyes, Born equation with dielectric saturation	$-108.$	$-1110$	
1963	Halliwall and Nyburg, dominant charge- quadrupole interaction		$-1090 + 10$	
1978	Conway, review of various methods	$-1070 \pm 20$	$-1100 + 20$	
1985 -	Reiss and Heller, electrochemical (abs. potential of H <sub>2</sub> /H <sup>+</sup> electrode)	$-1080 + 10$		
1987	Marcus, physical organic ( $PhaAs+$ = $PhaB-$		$-1100 \pm 10$	
1994	Marcus, review, average	$-1060$	$-109_{5}$	
dissections	Standard deviation of these	12	6	

Table 3.  $\Delta G^0$  and  $\Delta H^0$  for H<sup>+</sup> (g, atm)  $\rightarrow$  H<sup>+</sup> (aq, molal).

All available data for  $\Delta G_{\text{hyd}}^0$  for neutral pairs can be separated into ionic terms  $\Delta G_{\text{avg}}^0$  (J<sup>+</sup>) if a single absolute value for an ionic species can be deduced; that is, there is just one parameter. In table 3 this parameter is chosen to be  $\Delta G_{\text{hyd}}^0$  (H<sup>+</sup>), an essential ingredient for basicity and hydronium-hydrate reactivity in the gas phase (Hierl *et al.*  1988, Koppel *et al.* 1994, Smith *et al.* 1980). Because of the concordance of the largely independent approaches and because, save for one parameter, the material is experimental, we think of the values of  $\Delta G_{\text{hyd}}^0$  (J<sup>+</sup>) as essentially experimental values, with a determinate error that is probably within 20  $kJ$  mol<sup>-1</sup>. Of course, 20  $kJ$  mol<sup>-1</sup> is large on the scale of RT, but it is small compared to the magnitude of the values obtained for  $\Delta G_{\text{hyd}}^0$  (J<sup>+</sup>). In the following we shall use the values listed in table 2, which are based on the Marcus review (1994); they differ little from the values reported by Latimer *et al.* (1939).

The difference in energy stored in the electric fields *(E>* associated with a solution phase (M) and a gas phase (g) system is given by

$$
\Delta W_{\text{elec}} = \frac{N_A \varepsilon_0}{2} \int [D_M(E) E_M^2 - D_g(E) E_g^2] dV, \qquad (4a)
$$

where  $\varepsilon_0$  is the permittivity of free space,  $N_A$  is Avogadro's number, and *D* is the dimensionless dielectric constant or relative permittivity (Bottcher 1952). In the particular case of interest where the fields are associated with an ion having spherical symmetry and charge  $q_{\text{J}}$ , for which  $E = q_{\text{J}}/[4\pi\varepsilon_0 D(E)r^2]$ , equation (4*a*) becomes

$$
\Delta W_{\text{elec}} = \frac{q_j^2 N_A}{8\pi\varepsilon_0} \int \left[ \frac{1}{D_M(r)} - \frac{1}{D_g(r)} \right] \frac{dr}{r^2}.
$$
 (4b)

In principle *D* is a function of the electric field and thus in the case of the spherical ion

*D* is also a function of *r,* the distance from the centre of the ion. Note also that by electrostatic definition,  $q<sub>j</sub>$  is the free charge and  $q<sub>j</sub>/D(r)$  is the net charge. That is,  $q<sub>1</sub>/D(r)$  is the difference between the free charge and the screening charge (which will also have spherical symmetry) resulting from the polarization of the dielectric around the ion.

The application of equation  $(4b)$  to the determination of the electrical part of the hydration free energy of  $J^{\pm}$  NSG can be seen with the aid of figure 2. Because of dielectric saturation at distances close to  $r_1$ ,  $D_M(r)$  will not yet have reached its conventional low-field value,  $(D_M = 78.3$  for water). However if electrical saturation is nearly complete for  $r \ge r_2$ , then beyond NS  $D_M \approx 78.3$ . Also, since we are assuming for now that the structures NSG and NSL are the same, when  $r < r_2$ ,  $D_g(r) = D_M(r)$ , while  $D_{\varrho}(r) = 1$  for  $r > r_2$ . In this case equation (4b) becomes

$$
\Delta W_{\text{elec}} = \frac{q_{\text{J}}^2 N_{\text{A}}}{8\pi\epsilon_0} \left[ \int_{r_1}^{r_2} \left( \frac{1}{D_M(r)} - \frac{1}{D_g(r)} \right) \frac{dr}{r^2} + \int_{r_2}^{\infty} \left( \frac{1}{D_M} - 1 \right) \frac{dr}{r^2} \right]
$$
(5a)

$$
= \Delta W_{\text{elec, inner}} + \frac{694.5}{r_2} \left[ 1 - \frac{1}{D_M} \right]
$$
 (5b)

where  $\Delta W_{\text{elec, inner}}$  should be equal to zero when NSG = NSL. In equation (5b)  $r_2$  is measured in A. But before using this equation we have to show that electrical saturation is indeed nearly negligible when  $r \ge r_2$ .

The smallest  $r_2$  in table 2 is 3.09 A for Li<sup>+</sup> . NSG. The local dielectric constant in an electric field at a distance of 3.09 A from the centre of a univalent ion in water is calculated conveniently by the method of Booth (1951), who introduced a Langevin factor for dielectric saturation into Oster and Kirkwood's model (1943) for the dielectric constant of water. Within that framework, Booth's calculation of *D(E)* is a close approximation. The range of electrical saturation in water is shorter than originally predicted by Debye (1945). After minor adjustment of the dipole moment of the water molecule to fit  $D = 78.3$  in low electric fields at 298 K,  $D(r)$  at a distance *r* from the ionic centre was calculated from Booth's  $D(E)$  and the relation  $r^2D_M(r)$  =  $r^2 \cdot D_M(E) = q_J/4\pi\epsilon_0 E$ . For the smallest *r* of interest, 3.09 A,  $D_M(r) = 68$ . Accordingly, the factor  $(1 - 1/D<sub>M</sub>)$  in the Born equation varies between  $(1 - 1/68) = 0.985$ , and  $(1 - 1/78.3) = 0.987$ . The error of neglecting this variation in Born integrals is less than 0.2 *Yo.* 

**A** different way of suggesting that the bulk dielectric constant, 78.3, is a plausible choice when  $r > r<sub>9</sub>$ , is to interpret the dissection method first used by Latimer *et al.* in 1939 for ions  $J^{\pm}$ . If  $D_{\bf w}$  was constant (= 78.3) for all radii up to the ionic radius and if  $\Delta W_{\text{elec}}$  was the only contributor to the hydration free energy, then we would immediately have from equation (4b),

$$
\Delta G_{\text{hyd}}^{0} \left( \frac{M^{+} + X^{-}}{M} \right) / k \text{J} \text{ mol}^{-1} = 694.5(1/78.3 - 1)(1/r_{1+} + 1/r_{1-}), \text{ with } r \text{ in } \text{\AA}. \tag{6a}
$$

Latimer *et al.* (1939) found that this gave poor agreement with the experimental data; when the  $r_{1+}$  and  $r_{1-}$  where chosen as the Pauling ionic crystal radii, the calculated values of  $\Delta G_{\text{hyd}}^0$  were much too large. However, agreement was greatly improved when the above equation was replaced by

$$
\Delta G_{\text{hyd}}^{0} \left( \mathbf{M}^{+} + \mathbf{X}^{-} \right) = 694.5(1/78.3 - 1)[1/(r_{1+} + \delta_{+}) + 1/(r_{1-} + \delta_{-})]. \tag{6b}
$$

In this modified equation,  $\delta_+$  was a constant parameter for all cations and  $\delta_-$  was constant for all anions. They reported  $\delta_+ \approx 0.85$  Å and  $\delta_- \approx 0.1$  Å.  $\Delta G_{\text{hyd}}^0$  (M<sup>+</sup>) is then



Figure **3.** Hydration free energies of alkali *(0)* and halide ions **(m)** in comparison with the calculated free energies (electrostatic and surface) associated with the process,  $J^{\pm}$  (g)  $\rightarrow$  $J^{\pm}$  · NSG (g).

assigned the value  $694.5(1/78.3 - 1)(1/(r_{1+} + \delta_+))$  and  $\Delta G_{\text{hyd}}^0$  (X<sup>-</sup>) the value 694.5(1/78.3 - 1) (1/ $(r_1 + \delta)$ ). The  $\delta s$  are notably smaller than the thickness, 2.4 A, of the nearest-neighbour shell. In carrying out the integration demanded by  $(4b)$ , it is clear that we only have to integrate over volume elements in which  $D<sub>M</sub>$  differs from  $D<sub>g</sub>$ .

## *3.2. Surface work*

Consider a spherical droplet of radius *r.* Let *r* be small enough so that the thickness *t* of the surface 'phase' around the droplet is significant, and let  $(r - t)$  be the radius of the interior liquid. Let  $f_{\text{int}}$  denote the fraction of  $(4/3)\pi r^3$ , the total volume, that belongs to the interior. Then  $f_{\text{int}} = (1 - t/r)^3$ , and  $f_{\text{surf}} = (1 - f_{\text{int}})$ . Let  $\gamma_r$  denote the surface tension, which is a function of  $r$  defined so that it applies when the surface area  $A=4\pi r^2$ .

The surface work now consists of two parts. The fraction  $f_{\text{surf}}$  of the droplet has its free energy raised by  $4\pi r^2 y_r$ . The surface tension  $\gamma_r$  in turn compresses the interior, and the pressure increase, as predicted by the Kelvin equation, is  $\delta P = 2\gamma_r/r$ . The fraction  $f_{\text{int}}$  of the droplet therefore has its free energy raised by  $V_{\text{int}} \delta P$ , or  $(4/3)\pi (r-t)^3 (2\gamma_r/r)$ . The total work *per mole* of droplets is given by

$$
\Delta W_{\rm surf} = N_A f_{\rm surf} \cdot 4\pi r^2 \gamma_r + N_A f_{\rm int} \cdot (8\pi/3) \gamma_r (r-t)^3 / r. \tag{7}
$$

There are two limiting cases. (a) When  $t \ll r$ ,  $f_{\text{surf}}$  is negligible and  $\Delta W_{\text{surf}} =$  $N_A(8\pi/3) \gamma_r r^2$ . This is the Kelvin equation for macroscopic droplets. (b) When  $t \approx r$ ,  $f_{\text{int}}$  is negligible, the droplet is so small that  $f_{\text{surf}} \approx 1$  and  $\Delta W_{\text{surf}} = 4\pi N_A \gamma_r r^2$ . Cases (a) and (b) differ by only  $\frac{2}{3}$ . For the species  $J^{\pm}$  ·NSG that we are considering, case (b) applies. Also, as *r* decreases, it is likely that *y,* decreases somewhat below *y* (Lewis and Randall 1961, Boruvka *et al.* 1985), the conventional surface tension for a flat surface. In the following figure 3, we have assumed that for the species  $J^{\pm}$   $\cdot$  NSG,  $\gamma_r/\gamma = \frac{2}{3}$ .

## **4. Interpretation**

Calculated values for  $\Delta W_{elec}$  and  $\Delta W_{surf}$ , using equations (5b) and (7; case (b)), together with the data for  $\Delta G_{\text{hyd}}^0$  (J<sup>+</sup> · NSG) are displayed in figure 3. The plotted points and smooth relationships confirm that the hydration free energies are significant and are mostly accounted for by the Born term (dotted curve), with surface tension amounting to less than one-third of the total for the halide ions, and less than onetenth for the alkali ions. The calculated values of  $(\Delta W_{\text{elec}} + \Delta W_{\text{surf}})$  (solid curve) differ from  $-\Delta G_{\text{hyd}}^0$  (J<sup> $\pm$ </sup> ·NSG) by an average of 35 kJ mol<sup>-1</sup>, the calculated values being too negative for the cations and not negative enough for the anions.

A key assumption so far has been that  $NSG = NSL$ , which implies that  $\Delta W_{\text{elec, inner}} = 0$ . If this assumption were wrong and if the solid curve and points in figure 3 were error-free,  $\Delta W_{elec,inner}$  would be measured by the distances of the points from the solid curve, and thus would be substantial. We do not believe that. While AWelec,inner may not be zero, we would expect the structures **NSG** and NSL to be similar since they are both under the influence of the strong ion field.

Another intriguing aspect of figure 3 is that the values for  $\Delta G_{\text{pvd}}^0$  (J<sup>±</sup> · NSG) clearly divide into two sets-one for anions and one for cations, with a separation of about 100 kJ mol<sup>-1</sup>. A similar dispersion into two sets has long been known for  $\Delta G_{\text{hvd}}^0$  (J<sup>±</sup>) of the bare alkali and halide ions (Latimer **et al. 1939),** and one may wonder if such dispersion stems from a qualitative difference in the structure of nearest-neighbour shells. The evidence, like so much evidence in the field of hydration, is ambiguous. On the one hand, if there were a chemical origin, dispersion should show up also in a plot of  $\Delta G_n^0$  for alkali and halide ions. A careful examination of all Kebarle's data (1970) for both  $\Delta H_w^0$  and  $\Delta G_w^0$  however offers no convincing evidence for such dispersion.

On the other hand, the surface work implied by the distances between the dotted curve for  $\Delta W_{elec}$  and the points for  $\Delta G_{\text{hvd}}^0$  in figure 3 may well supply a clue. Let us first ignore the solid curve because the estimate of  $\Delta W_{\text{surf}}$  via equation (7; case (b)) is not reliably accurate for extremely small 'droplets' such as  $M^+$  NSG and  $X^-$  NSG. Surface tension is basically an intermolecular phenomenon whose existence requires the truncation of intermolecular interactions at the phase boundary (Millikan **et al. 1937)** : when there are no intermolecular interactions, there is no surface tension. Suppose, for example, that the ion and the *n* adjacent water molecules form a molecular complex (rather than a cluster consisting of  $n + 1$  separate particles). The ion hydrate is then a single molecule, and whatever energy might be assigned to the surface of that molecule is part of the intrinsic energy of the molecule. There is no distinct, specifiable surface energy, and  $\Delta W_{\text{surf}}$  accordingly is zero. Figure 3 shows that this description is a viable zeroth approximation for the alkali ions, especially for  $Li<sup>+</sup>$  and Na+.

On the other hand, let the ion and the *n* adjacent water molecules exist as a cluster of  $n+1$  separate particles. Now there are intermolecular interactions and  $\Delta W_{surf}$  is non-zero. Following equation (7), the *n* water molecules are part of the surface layer, and the ion is in the interior; hence case (b) nearly applies. Assuming that  $\gamma_r/\gamma = \frac{2}{3}$ , we predict  $\Delta W_{\text{surf}} = (8\pi/3)N_A \gamma r_2^2$ , which yields the solid curve in figure 3. Making a reasonable allowance for the uncertainty in  $\gamma_r$ , figure 3 shows that the cluster hypothesis is a viable approximation for anions.

In conclusion, one can build a case that the pattern of the points in figure **3** can be rationalized if the alkali ions form molecular complexes with at least part of the **5-9**  water molecules in the nearest-neighbour shells, while the halide ions and their surrounding water molecules remain separate molecules. This case is not definitive, but it is consistent with other evidence based on rather different properties. For instance, the ionic conductivities of  $Li<sup>+</sup>$  and  $Na<sup>+</sup>$  in solution are low, relative to the bare-ion size, in contrast to those of halide ions; for a recent example, see D'Aprano **et** *al.* **(1995).** The absorption mode in dielectric relaxation in aqueous salt solutions shows that some water molecules are irrotationally bound to alkali ions but not to halide ions (Haggis *et* **al. 1952).** There is thermodynamic and **NMR** evidence that alkali ions, but not halide ions, form complexes with organic solvent molecules in

water-organic mixed solvents (Grunwald *er al.* 1960, Fratiello *er* al. 1968). And the hydration-shell water molecules of many di- or higher-valent cations reside next to the cations long enough to give discrete NMR spectra, while the authors know of no such evidence for di- or higher-valent anions (Gordon 1975).

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#### **References**

- **ARSHADI,** M., YAMDAGNI, R., and KEBARLE, P., 1970, J. *phys. Chem.,* 74, 1475.
- BOTTCHER, C. J. F., 1952, *Theory of Electric Polarisation* (Amsterdam: Elsevier).
- BOOTH, F., 1951, J. *chem. Phys.,* 19,391, 1327, 1615.
- BORN, M., 1920,Z. *Phys.,* 1,45.
- BORUVKA, L., ROTENBERG, Y., and NEUMANN, A.W., 1985, J. *phys. Chem.,* 89,2714.
- CONWAY, B. E., 1978, J. *solution Chem.,* **7,** 721.
- D'APRANO, A., SALOMON, M., and MAURO, V., 1995, J. *solution Chem.,* 24,685.
- DEBYE, P., 1945, *Polar Molecules* (New York: Dover).
- **DZIDIC,** I., and KEBARLE, P., 1970, J. *phys. Chem.,* 74, 1466.
- FAJANS, K., 1919, *Verh. Deutsch. Phys. Ges.,* 21, 13.
- FRATIELLO, A., LEE, R. E., VONE, M. N., and SCHUSTER,. E., 1968, J. *chem. Phys.,* 48,3705.
- GORDON, *J.* E., 1975, *Organic Chemistry of Electrolyte Solutions* (New York: Wiley) p. 175-8.
- GRUNWALD, E.,BAUGHMAN, G., and KOHNSTAM, G., 1960, *J.* Am. *chem. SOC.,* 82,5801.
- HAGGIS, *G.* H., HASTED, J. B., and BUCHANA, T. J. 1952, *J. chem. Phys.,* 20, 1452.
- HALLIWELL, H. F., and **NYBURG,** S. C., 1963, *Trans. Faraday Soc.,* 59,1126.
- HIERL, P. M., AHRENS, A. F., HENCHMAN, M. J., VIGGIANO, A. A., PAULSON, J.F., and CLARY, D. C., 1988, *Faraday Discuss. Chem. SOC.,* 85, 37.
- KOPPEL, I. A., ANVIA, F., and TAFT, R. W., 1994, *J. phys. org. Chem.,* 7, 717.
- LATIMER, W. M., PITZER, K. S., and SLANSKY, C. M., 1939, J. *chem. Phys.,* **7,** 108.
- **LEWIS,** G. N., and RANDALL, M., 1961, *Thermodynamics,* 2nd edn (New **York:** McGraw-Hill), Chap. 29.
- MARCUS, Y., 1987, J. *Chem. SOC. Faraday,* 1, *83,* 339.
- MARCUS, Y., 1994, *Biophys. Chem.,* **51,** 11 1.
- MILLIKAN, R. A., ROLLER, D., and WATSON, E. C., 1937, *Mechanics, Molecular Physics, Heat, and Sound* (Boston: Ginn & Co.) Chap. 13.
- NARTEN, A. H., and LEVY, H. A., 1969, *Science,* 165,447.
- NOYES, R. M., 1962, *J. Am. chem. Soc.*, 84, 513.
- **OSTER,** *G.,* and **KIRKWOOD,** J. G., 1943, *J. chem. Phys., 11,175.*
- **kiss, H.,** and HELLER, A., 1985, J. *phys. Chem.,* 89,4207.
- SMITH, *D.,* **ADAMS,** N. G., and HENCHMAN, M. J., 1980, J. *chem. Phys.,* 72,4951.